

## Lesson 5: M-I coupling and auroral arcs

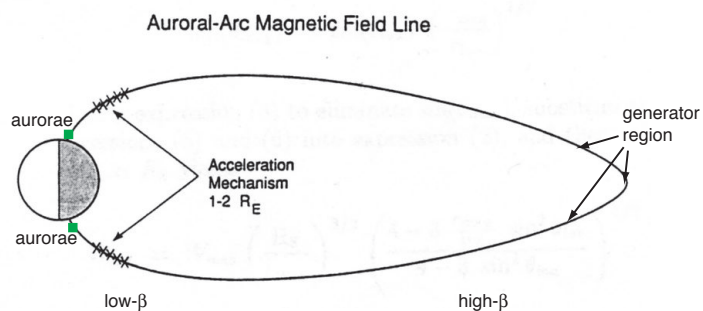
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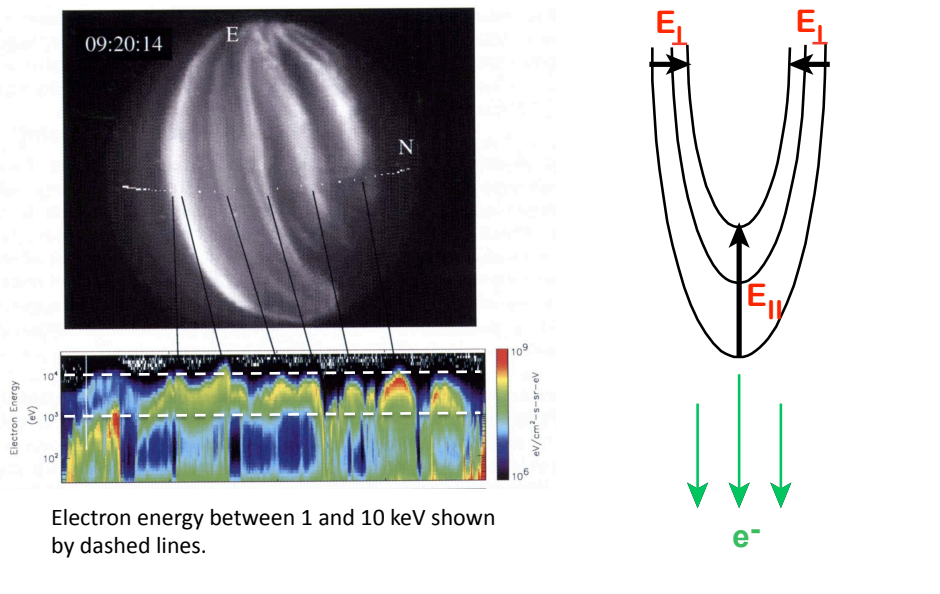
### Energy of particles in discrete aurora

Energy of plasma sheet and PSBL electrons is typically smaller than for electrons producing aurora in the ionosphere. Further energy may come from:

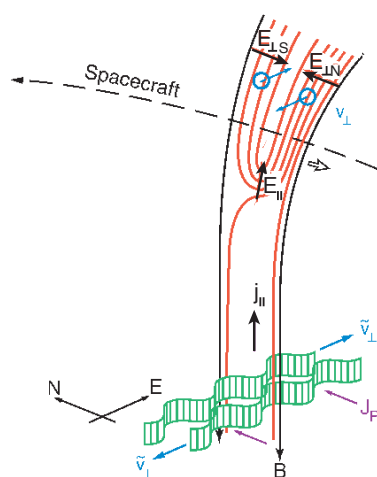
- Auroral acceleration region at altitudes of  $\sim 1 - 3 R_E$
- During substorms, from magnetic reconnection in the tail at NENL ( $X \sim 20-30 R_E$ )
- From waves, especially from kinetic/inertial Alfvén waves



### Acceleration of auroral particles by a quasi-static electric field structure (potential drop)



### U-shaped potential structure



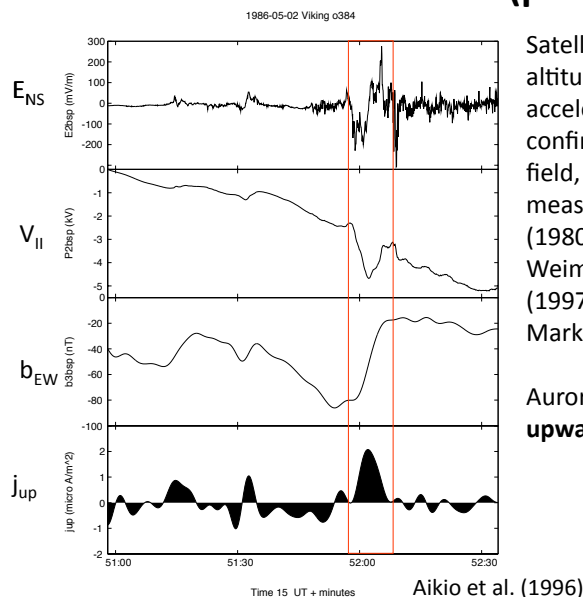
By integrating the electric field along the path, one gets the potential variation. Since  $V = \int \mathbf{E} \cdot d\mathbf{l}$  we get

$$\int E_{\perp N} dl_{\perp N} = \int E_{\parallel} dl_{\parallel} = -V_{\parallel}$$

and satellite measurement of electric field can yield the parallel potential drop  $V_{\parallel}$  below the satellite.

Electric fields (arrows), constant potential contours (red) and the upward field-aligned current in the *auroral acceleration region* (Auroral Plasma Physics, 2002).

## Acceleration of auroral particles by a quasi-static electric field structure (potential drop)



Satellite measurements at altitudes of 1-3  $R_E$  (the acceleration region) have confirmed the picture by electric field, particle and magnetic field measurements, e.g. Mozer et al. (1980), Temerin et al. (1981), Weimer (1985), Marklund et al. (1997), Carlson et al. (1998), Marklund et al. (2001), ...

Auroral arcs are associated with **upward FAC** from the arc!

## Upward FAC and $V_{||}$

To find the relationship between  $j_{||}$  and  $V_{||}$  we need the kinetic theory (not MHD). Kinetic theory utilizes the particle distribution function  $f(\mathbf{r}, \mathbf{v}, t)$ , which is a concept of statistical physics. Knight (1973) and Lemaire and Scherer (1974) derived the current carried by magnetospheric electrons, undergoing adiabatic motions:

$$j_{||} = j_{th} \frac{B_i}{B_m} \left[ 1 - \left( 1 - \frac{B_m}{B_i} \right) \exp \left( - \frac{eV_{||}}{E_{th} \left( \frac{B_i}{B_m} - 1 \right)} \right) \right]$$

where  $B_i$  is the magnetic field at the ionospheric altitude and  $B_m$  is the magnetic field in the magnetosphere. The thermal current  $j_{th}$  is the current that is carried by precipitating electrons without any potential drop (it is carried by electrons, whose pitch angle in the equatorial plane is small enough so that their mirror point is down in the ionosphere and hence they are lost in the ionosphere):

$$j_{th} = en \left( \frac{E_{th}}{2\pi m_e} \right)^{\frac{1}{2}}$$

### Knight equation

When  $k_B T \ll eV_{\parallel} \ll \frac{B_i}{B_m} k_B T$ , the Knight equation can be approximated by

$$j_{\parallel} = \frac{ne^2}{(2\pi m_e E_{th})^{1/2}} V_{\parallel} = K V_{\parallel}$$

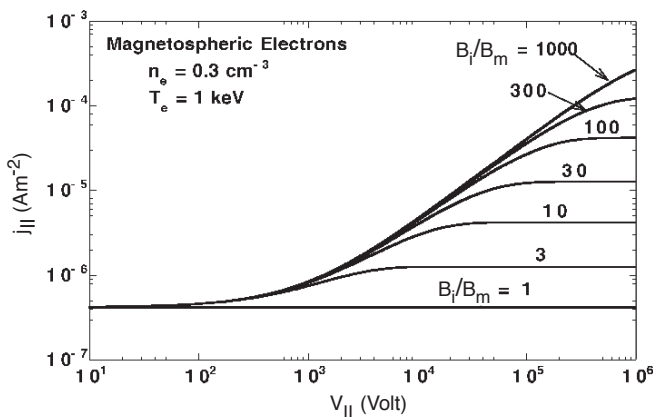


Figure: The field-aligned current density away from the ionosphere (upward) as a function of the parallel potential drop for various values of the mirror ratio  $B_i/B_m$ . Which part corresponds to the equation above?

### Current system associated with auroral arcs

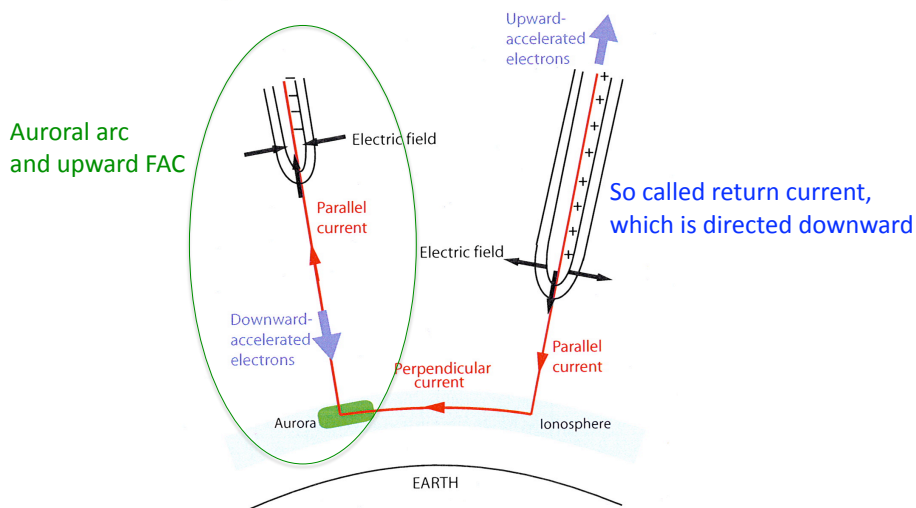
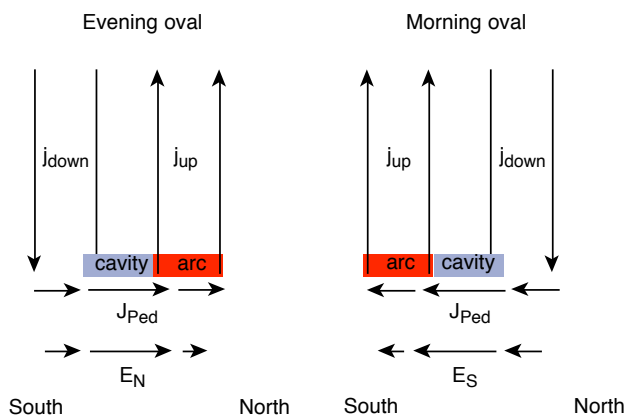


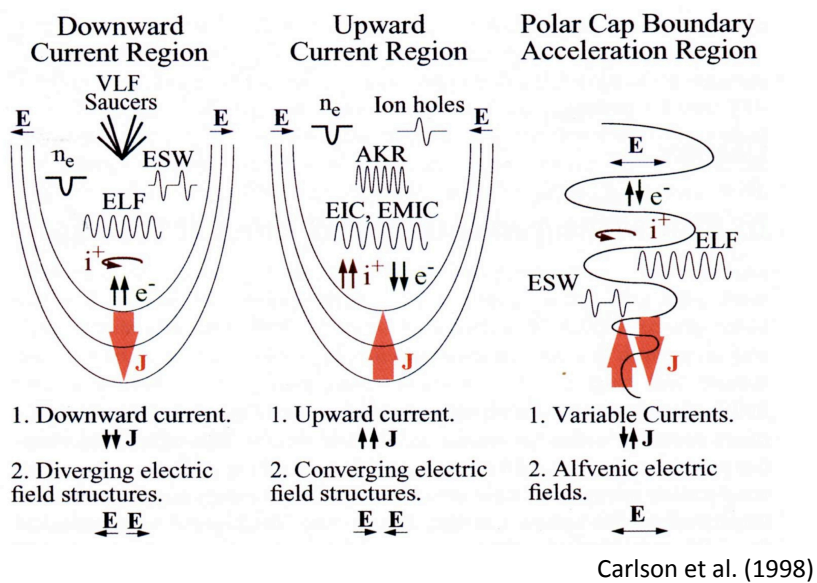
Figure 7.3: Schematic figure of the auroral current circuit with negative and positive potential structures corresponding to convergent and divergent high-altitude electric fields, respectively (Marklund, 2001).

### Arc current systems in the dusk and dawn oval



- Density cavity and the enhanced ionospheric electric field are not always observed
- An auroral arc and the upward FAC may be formed also at a convection reversal boundary.
- Opgenoorth et al. (1990), Aikio et al. (1993), Aikio et al. (2002)

### Schematics from high-altitude satellite measurements



### Acceleration of auroral particles by inertial Alfvén waves

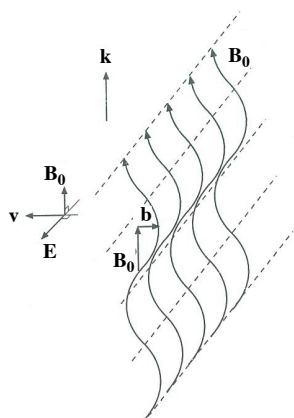
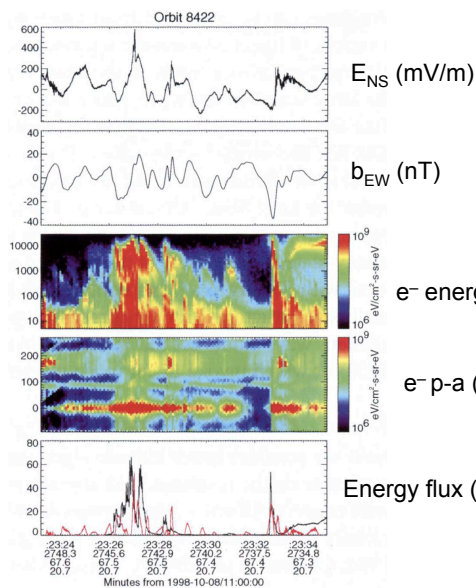


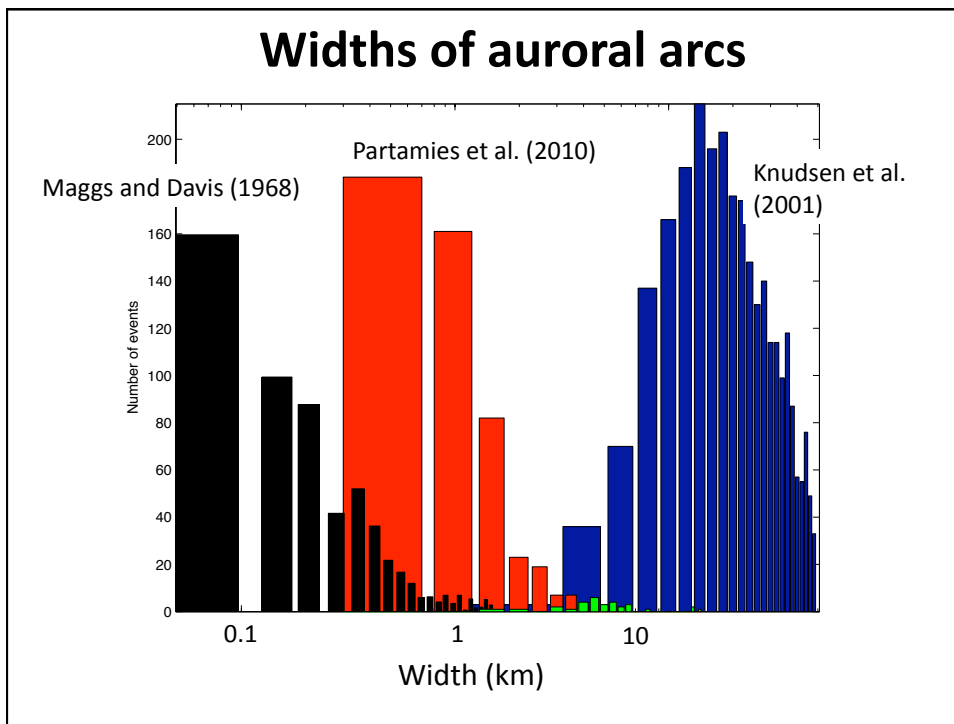
Figure: Shear Alfvén waves are transverse MHD plasma waves that travel along  $B$ .

When the perpendicular scale length of the Alfvén waves becomes too small, the ideal MHD breaks down and the waves become dispersive, which means that different frequencies travel at different velocities. This leads to a change in the nature of Alfvén waves, in particular a parallel wave electric field is introduced. This  $E_{||}$  may accelerate particles.

### Acceleration of auroral particles by inertial Alfvén waves



FAST satellite measurement of wave fields and electrons close to the nightside polar cap boundary at an altitude of about 2740 km showing evidence of inertial Alfvén waves and F-A electrons accelerated by the waves. Note that electron energy range is broad.



### Width of arc and all-sky image

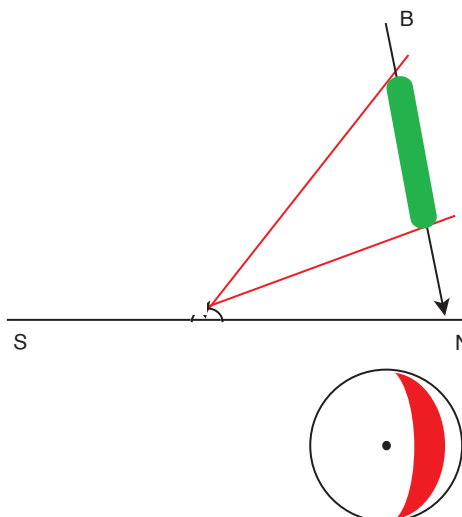
**Group task 5:** How does the 2D all-sky image map to the sky? Make a sketch in the magnetic meridian plane! Which of the two boundaries is the more important one for the location of the arc?

The diagram shows a circle representing the sky in the magnetic meridian plane. A red arc is drawn on the right side of the circle, representing an auroral arc. The left side of the circle is labeled 'S' (South) and the right side is labeled 'N' (North). A small black dot is located at the center of the circle.

## Result

All-sky camera measuring an auroral arc

When the arc is located to the north or to the south of the magnetic zenith, the width in the ASC image is an apparent width and only the outer boundary from the zenith gives an estimate of the location of the arc.

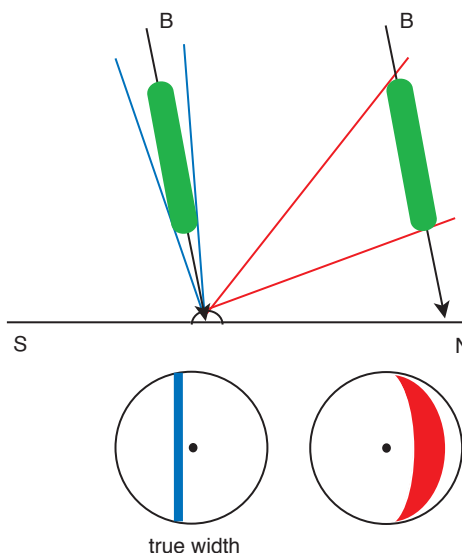


## How to measure true width?

All-sky camera measuring an auroral arc

When the arc is located to the north or to the south of the magnetic zenith, the width in the ASC image is an apparent width and only the outer boundary from the zenith gives an estimate of the location of the arc.

When the auroral arc (narrow in the north-south direction and with some vertical extent) is **in the magnetic zenith** and the camera is directed towards the magnetic zenith, the true width of the arc can be estimated.



## Some theoretical considerations related to observed widths of auroral arcs

**Electrostatic coupling** between the magnetosphere and the ionosphere:

- Natural scale length  $L$  of electrostatic mapping between the ionosphere and magnetosphere (Weimer, 1985) depends on Pedersen conductance  $\Sigma_p$  and field-line conductance  $K$

$$L = \sqrt{\frac{\Sigma_p}{K}} \quad \text{and } K \text{ is} \quad j_{\parallel} = \frac{ne^2}{(2\pi m_e E_{th})^{\frac{1}{2}}} V_{\parallel} = K V_{\parallel} ,$$

It has been estimated that  $L$  varies between **100 km** (e.g. Lysak, 1991) and 340 km (Borovsky, 1993) => large-scale inverted-V's could be explained.

## Some theoretical considerations related to observed widths of auroral arcs

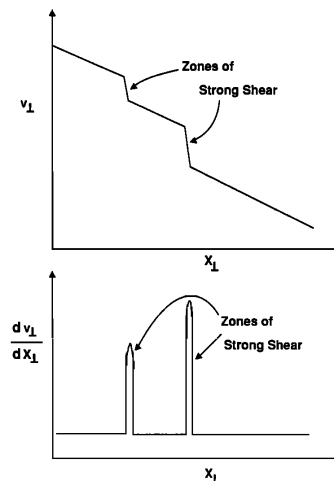
The parallel electric field in **inertial Alfvén wave** is given by:

$$\frac{E_{\parallel}}{E_{\perp}} = \frac{k_{\parallel} k_{\perp} \lambda_e^2}{1 + k_{\perp}^2 \lambda_e^2}$$

where  $\lambda_e$  is the electron skin depth and  $k_{\parallel}$  and  $k_{\perp}$  are parallel and perpendicular wavenumbers. Typically  $\lambda_e k_{\perp} \sim 1$ .  $E_{\parallel}$  can be 1 mV/m over wavelengths of more than 1000 km. The potential drop in the wavefront of the inertial Alfvén wave can be of the order of kilovolts, though more typically hundreds of eV. Typical widths are **~1 km**.

## Some theoretical considerations related to observed widths of auroral arcs

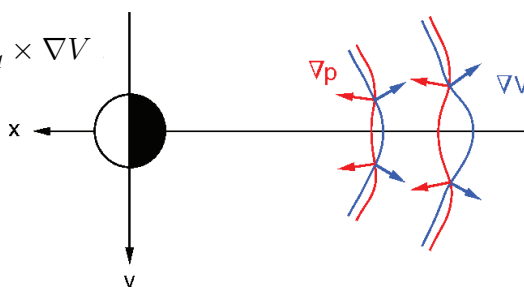
**Velocity shears** (plasma vorticity given by  $\nabla \times \mathbf{v}$ ) can act as a MHD generator and drive F-A currents. Borovsky (1993) estimated that typical shear widths in the low-latitude boundary layer (LLBL) give widths of **~130 km** and in the plasma sheet **3 – 50 km**.



## Some theoretical considerations related to observed widths of auroral arcs

**Pressure gradients** in the plasma sheet may be associated with FAC:

$$\frac{j_{\parallel}^{ion}}{B} = -\frac{\mathbf{B}_{eq}}{B_{eq}^2} \cdot \nabla p_{eq} \times \nabla V$$



Borovsky (1993) estimated that for 4 keV ions in the plasma sheet ( $X = -12 R_e$ ) the minimum pressure gradient width (corresponding to ion gyroradius) would map to a value of **~3 km** in the ionosphere.

## Some theoretical considerations related to observed widths of auroral arcs

**Conclusion:** Several mechanisms produce auroral arcs with widths above 1 km, but **small-scale (< 1 km)** widths are difficult to explain!

## Summary

Ground-based optical observations show that multiple scale structures are often observed in aurora.

To explain those, probably several different generation and acceleration mechanisms are needed.

**At the moment, we don't know the process to produce auroral arcs => Key challenge for magnetosphere-ionosphere coupling studies.**

